

# GUIDANCE FOR THE SURVEY AND CONSTRUCTION OF STEEL SHIPS

## Part D

## Machinery Installations

Guidance for the Survey and Construction of Steel Ships

Part D

2014 AMENDMENT NO.3

Notice No.68      19th December 2014

Resolved by Technical Committee on 29th July 2014

**ClassNK**  
NIPPON KAIJI KYOKAI

Notice No.68 19th December 2014

## AMENDMENT TO THE GUIDANCE FOR THE SURVEY AND CONSTRUCTION OF STEEL SHIPS

“Guidance for the survey and construction of steel ships” has been partly amended as follows:

### **Part D MACHINERY INSTALLATIONS**

#### Amendment 3-1

#### **Annex D1.1.3-3 GUIDANCE FOR THE SURVEY AND CONSTRUCTION OF AZIMUTH THRUSTERS**

##### **1.2 Class Surveys**

##### **1.2.2 Periodical Surveys**

Sub-paragraph -4 has been amended as follows.

#### **4 Docking Surveys**

- (1) Visual inspections of steering columns, propeller pods and propellers (including bolt locking and other fastening arrangements) are to be carried out.
- (2) Examinations on sealing devices for azimuth steering gears ~~and~~, propeller shafts and propeller blades are to be carried out.
- (3) Measurements of the wear down of the bearing are to be carried out. (Except when roller bearings are used as bearings for propeller shafts)

#### EFFECTIVE DATE AND APPLICATION (Amendment 3-1)

1. The effective date of the amendments is 19 December 2014.
2. Notwithstanding the amendments to the Guidance, the current requirements may apply to the surveys for which the application is submitted to the Society before the effective date.

## Annex D5.3.5 GUIDANCE FOR CALCULATION OF STRENGTH OF GEARS

Section 1.2 has been amended as follows.

### 1.2 Symbols and Units

The main symbols introduced in this Guidance are listed below.

( $a$  to  $Y_\beta$  are omitted)

$Y_B$  = rim thickness factor

$s_R$  = rim thickness of gears (mm)

$h$  = tooth height (mm)

$Y_{DT}$  = deep tooth factor

$K_{F\alpha}$  = transverse load distribution factor for tooth root bending stress

$K_{F\beta}$  = face load distribution factor for tooth root bending stress

$\sigma_{FP}$  = permissible tooth root bending stress ( $N/mm^2$ )

$\sigma_{FE}$  = bending endurance limit ( $N/mm^2$ )

$Y_N$  = life factor for tooth root bending stress

$Y_d$  = design factor

$Y_{\delta relT}$  = relative notch sensitivity factor

$q_s$  = notch parameter

$\rho'$  = slip-layer thickness (mm)

$Y_{RrelT}$  = relative surface factor

$Y_X$  = size factor for tooth root bending stress

$S_F$  = safety factor for tooth root bending stress

Section 1.3 has been amended as follows.

### 1.3 Geometrical definitions

In the case of internal gearing  $z_2$ ,  $a$ ,  $d_2$ ,  $d_{a2}$ ,  $d_{b2}$  and  $d_{w2}$  are negative. The pinion is defined as the gear with the smaller number of teeth; therefore, the absolute value of the gear ratio, defined as follows, is always greater or equal to the unity.

$$u = \frac{z_2}{z_1} = \frac{d_{w2}}{d_{w1}} = \frac{d_2}{d_1}$$

In the case of external gears,  $u$  is positive. In the case of internal gears,  $u$  is negative. In the equation of surface durability,  $b$  is the common facewidth on the pitch diameter. In the equation of the tooth root, bending stress  $b_1$  or  $b_2$  are the facewidths at their respective tooth roots. In any case,  $b_1$  and  $b_2$  are not to be taken as greater than  $b$  by more than one module ( $m_n$ ) on either side. The common facewidth  $b$  may be used also in the equation of teeth root bending stress if either

significant crowning or end relief has been adopted.

$$\tan \alpha_t = \frac{\tan \alpha_n}{\cos \beta}$$

$$\tan \beta_b = \tan \beta \cos \alpha_t$$

$$\frac{d}{\cos \beta} = d_{1,2} = \frac{z_{1,2} m_n}{\cos \beta}$$

$$\frac{d_b}{\cos \alpha_t} = \frac{d_w}{\cos \alpha_{tw}} \quad d_{b1,2} = d_{1,2} \cos \alpha_t$$

$$\left. \begin{aligned} d_{w1} &= \frac{2a}{u+1} \\ d_{w2} &= \frac{2au}{u+1} \end{aligned} \right\} \text{where } a = 0.5(d_{w1} + d_{w2})$$

$$\frac{z}{\cos^2 \beta_b \cos \beta} = z_{n1,2} = \frac{z_{1,2}}{\cos^2 \beta_b \cdot \cos \beta}$$

$$m_t = \frac{m_n}{\cos \beta}$$

$$\text{inv } \alpha = \tan \alpha - \frac{\pi \alpha}{180}; \alpha(^{\circ})$$

$$\text{inv } \alpha_{tw} = \text{inv } \alpha_t + 2 \tan \alpha_n \frac{x_1 + x_2}{z_1 + z_2}$$

or

$$\cos \alpha_{tw} = \frac{m_t (z_1 + z_2)}{2a} \cos \alpha_t$$

$$\varepsilon_{\alpha} = \frac{0.5 \sqrt{d_{a1}^2 - d_{b1}^2} \pm 0.5 \sqrt{d_{a2}^2 - d_{b2}^2} - a \sin \alpha_{tw}}{\pi m_t \cos \alpha_t}$$

A positive sign is used for external gears, a negative sign for internal gears.

$$\varepsilon_{\beta} = \frac{b \sin \beta}{\pi m_n}$$

In the case of double helix gears,  $b$  is to be taken as the width of one helix.

$$\varepsilon_{\gamma} = \varepsilon_{\alpha} + \varepsilon_{\beta}$$

$$\frac{v}{19099} = v = \frac{\pi \cdot d_{1,2} n_{1,2}}{60 \cdot 10^3}$$

Section 1.4 has been amended as follows.

#### 1.4 Nominal Tangential Load, $F_t$

Nominal tangential loads  $F_t$  which are tangential to cylinders and perpendicular to planes are to be calculated directly from the maximum continuous power transmitted by gear sets using the following equations:

$$T_{1,2} = \frac{9549 P}{n_{1,2}} \quad T_{1,2} = \frac{30 \cdot 10^3 P}{\pi \cdot n_{1,2}}$$

$$F_t = 2000 \frac{T_{1,2}}{d_{1,2}}$$

## 1.5 Loading Factors

Paragraph 1.5.1 has been amended as follows.

### 1.5.1 Application Factor, $K_A$

1 The application factor  $K_A$  accounts for dynamic overloads from source external to the gearing. The value  $K_A$  for gears designed for infinite lifespans is defined as the ratio between maximum repetitive cyclic torques applied to gear sets and nominal rated torques. Nominal rated torque is defined by rated power and speed and is the torque used in rating calculations. This factor mainly depends on:

- (1) The characteristics of driving and driven machines;
- (2) The ratio of masses;
- (3) The type of couplings;
- (4) Operating conditions (over speed, changes in propeller load conditions, etc.)

2 In cases where drive systems are operating at level near their critical speed, a careful analysis of conditions is to be made. The application factor  $K_A$  is to be determined either by direct measurements or by a system analysis that is acceptable to the Society. In cases where values determined in such ways cannot be provided, the following values may be used:

- (1) Main propulsion
  - $K_A = 1.00$  (diesel engines with hydraulic or electromagnetic slip couplings)
  - $= 1.30$  (diesel engines with high elasticity couplings)
  - $= 1.50$  (diesel engines with other couplings)

However, in cases where vessels, on which reduction gear is being used, are receiving Ice Class Notation, as required in 5.6, Part I of the Rules ~~the following value is to be substituted for the values given above for  $K_A$ .~~

$$K_A = \frac{1.10 \cdot M}{1 + J_1 / J_h \cdot M_0}$$

~~The values for  $J_1$ ,  $J_h$ ,  $M$  and  $M_0$  are the same as those specified in 5.4.5, Part I of the Rules.~~

- (2) Auxiliary gears
  - $K_A = 1.00$  (electric motors, diesel engines with hydraulic or electromagnetic slip couplings)
  - $= 1.20$  (diesel engines with high elasticity couplings)
  - $= 1.40$  (diesel engines with other couplings)

Paragraph 1.5.3 has been amended as follows.

### 1.5.3 Internal Dynamic factor, $K_V$

1 The internal dynamic factor  $K_V$  accounts for those internally generated dynamic loads due to vibrations of pinions and wheels against each other. The value  $K_V$  is defined as the ratio between those maximum loads which dynamically act on tooth flanks and maximum externally applied loads

( $F_t K_A K_v$ ). This factor mainly depends on:

- (1) Transmission errors depending on pitch and profile errors;
- (2) Masses of pinions and wheels;
- (3) Gear mesh stiffness variations as gear teeth pass through meshing cycles;
- (4) Transmitted loads including application factors;
- (5) Pitch line velocities;
- (6) Dynamic unbalance of gears and shafts;
- (7) Shaft and bearing stiffness;
- (8) Damping characteristics of gear systems.

2 The internal dynamic factor  $K_v$  is to be calculated as follows; however, this method is to be applied only to cases where all of the following conditions (1) to (4) are satisfied:

~~(1) Steel gears of heavy rims sections~~

~~(2)  $\frac{F_t}{b} > 150(N/mm)$~~

~~(3)  $z_1 < 50$~~

~~(4)~~ Running speeds in the following subcritical ranges:

~~$\frac{vz_1}{100} < 14$  (In the case of helical gears)~~

~~$\frac{vz_1}{100} < 10$  (In the case of spur gears)~~  $\frac{v \cdot z_1}{100} \sqrt{\frac{u^2}{1+u^2}} < 10$  (m/s)

~~(2)  $\beta = 0^\circ$  (In the case of spur gears)~~

~~$\beta \leq 30^\circ$  (In the case of helical gears)~~

~~(3) pinion with relatively low number of teeth:~~

~~$z_1 < 50$~~

~~(4) solid disc wheels or heavy steel gear rim~~

This method may be applied to all types of gears, if  ~~$\frac{vz_1}{100} < 3$~~   $\frac{v \cdot z_1}{100} \sqrt{\frac{u^2}{1+u^2}} < 3$  (m/s), as well as to

helical gears where  $\beta > 30^\circ$ . In the case of gears other than those given above, the value of  $K_v$  is to be determined, in consideration of results of analyses, by the Society on a case by case basis.

(a) For those helical gears with an overlap ratio  $\leq \geq$  unity and spur gears, the value of  $K_v$  is to be determined as follows:

~~$$K_v = 1 + \psi \frac{vz_1}{100}$$~~

$$K_v = 1 + \left( \frac{K_1}{K_A \frac{F_t}{b}} + K_2 \right) \cdot \frac{v \cdot z_1}{100} K_3 \sqrt{\frac{u^2}{1+u^2}}$$

~~The values of  $\psi$  are given in the following Table 5.3-1~~

$K_1$  : Factor specified in **Table 5.3-1.**

$K_2$  : Factors for all ISO accuracy grades. Values are as follows:

= 0.0193 (In the case of spur gears)

= 0.0087 (In the case of helical gears)

$K_3$  : Values are to be calculated by following formula:

$$= 2.0 \left( \frac{v \cdot z_1}{100} \sqrt{\frac{u^2}{1+u^2}} \leq 0.2 \right)$$

$$= 2.071 - 0.357 \cdot \frac{v \cdot z_1}{100} \sqrt{\frac{u^2}{1+u^2}} \left( \frac{v \cdot z_1}{100} \sqrt{\frac{u^2}{1+u^2}} > 0.2 \right)$$

If  $K_A \frac{F_t}{b}$  is less than 100 N/mm, this value is assumed to be equal to 100 N/mm.

(b) In the case of helical gears with an overlap ratio < unity, the value of  $K_V$  is to be obtained by means of linear interpolation as follows:

$$K_V = K_{V2} - \varepsilon_\beta (K_{V2} - K_{V1})$$

$K_{V1}$  : The values for helical gears specified in ~~Table 5.3-1~~ accordance with (a)

$K_{V2}$  : The values for spur gears specified in ~~Table 5.3-1~~ accordance with (a)

In the case of mating gears with different grades of accuracy, the grade corresponding to the lower accuracy is to be used.

~~Table 5.3-1~~ Values of  $\psi$

Type of gears	ISO grades of accuracy					
	3	4	5	6	7	8
Spur gears	0.022	0.030	0.043	0.062	0.092	0.125
Helical gears	0.0125	0.0165	0.0230	0.0330	0.0480	0.0700

Table 5.3-1 Values of  $K_1$

Type of gears	ISO grades of accuracy					
	3	4	5	6	7	8
Spur gears	2.1	3.9	7.5	14.9	26.8	39.1
Helical gears	1.9	3.5	6.7	13.3	23.9	34.8

## 1.6 Surface Strength

Paragraph 1.6.2 has been amended as follows.

### 1.6.2 Equations for Basic Contact Stress

(-1 is omitted)

#### 2 Single Pair Mesh Factors $Z_B$ and $Z_D$

The single-pair mesh factors  $Z_B$  for pinions and  $Z_D$  for wheels account for the influence on contact stress of tooth flank curvatures at inner points of single pair contacts. These factors transform those contact stresses determined at pitch points to contact stresses considering flank curvatures at inner points of single pair contacts. The values for  $Z_B$  and  $Z_D$  are to be determined as follows:

- (1) In the case of spur gears, the value for  $Z_B$  is to be taken as 1.0 or given by the following expression, whichever is greater.

$$M_1 = \frac{\tan \alpha_{tw}}{\left[ \sqrt{\left(\frac{d_{a1}}{d_{b1}}\right)^2 - 1 - \frac{2\pi}{z_1}} \right] \left[ \sqrt{\left(\frac{d_{a2}}{d_{b2}}\right)^2 - 1 - (\varepsilon_\alpha - 1) \frac{2\pi}{z_2}} \right]}^{\frac{1}{2}}$$

- (2) In the case of helical gears with  $\varepsilon_\beta \geq 1$ , the value for  $Z_B$  is to be taken as 1.0;  
(3) In the case of helical gears with  $\varepsilon_\beta > 1$ , the value for  $Z_B$  is to be taken as 1.0 or given by the following formula, whichever is greater:

$$Z_B = M_1 - \varepsilon_\beta (M_1 - 1)$$

- (4) In the case of spur gears, the value for  $Z_D$  is to be taken as 1.0 or given by the following expression, whichever is greater.

$$M_2 = \frac{\tan \alpha_{tw}}{\left[ \sqrt{\left(\frac{d_{a2}}{d_{b2}}\right)^2 - 1 - \frac{2\pi}{z_2}} \right] \left[ \sqrt{\left(\frac{d_{a1}}{d_{b1}}\right)^2 - 1 - (\varepsilon_\alpha - 1) \frac{2\pi}{z_1}} \right]}^{\frac{1}{2}}$$

- (5) In the case of helical gears with  $\varepsilon_\beta \geq 1$ ,  $Z_D$  is to be taken as 1.0.  
(6) In the case of helical gears with  $\varepsilon_\beta < 1$ ,  $Z_D$  is to be taken as 1.0 or given by the following formula, whichever is greater.

$$Z_D = M_2 - \varepsilon_\beta (M_2 - 1)$$

- (7) In the case of internal gears,  $Z_D$  is to be taken as 1.0.

### 3 Zone Factor, $Z_H$

The zone factor  $Z_H$  accounts for the influence on Herzian pressure of tooth flank curvatures at pitch points and relates those tangential forces at reference cylinders to those normal forces at pitch cylinders. The zone factor  $Z_H$  is to be calculated as follows:

$$\cancel{Z_H} = \frac{\sqrt{2 \cos \beta_b \cos \alpha_{tw}}}{\sqrt{\cos^2 \alpha_t \sin \alpha_{tw}}} \quad Z_H = \frac{\sqrt{2 \cos \beta_b}}{\sqrt{\cos^2 \alpha_t \tan \alpha_{tw}}}$$

(-4 and -5 are omitted)

### 6 Helix Angle Factor, $Z_\beta$

The helix angle factor  $Z_\beta$  accounts for the influence of helix angles on surface durability, allowing for such variables as distribution of loads along lines of contact.  $Z_\beta$  is dependent only on helix angles and its value can be obtained by the following formula:

$$\cancel{Z_\beta} = \sqrt{\cos \beta} \quad Z_\beta = \sqrt{\frac{1}{\cos \beta}}$$

where  $\beta$  is the reference helix angle.

Paragraph 1.6.3 has been amended as follows.

### 1.6.3 Permissible Contact Stress

(-1 is omitted)

#### 2 Endurance Limit for Contact Stress, $\sigma_{Hlim}$

For a given material,  $\sigma_{Hlim}$  is the limit of repeated contact stress which can be permanently endured. The value of  $\sigma_{Hlim}$  can be regarded as the level of contact stress which the material will endure without pitting for at least  ~~$50 \times 10^6$~~   $5 \times 10^7$  load cycles. "Pitting" is defined in the case of non surface hardened gears, the pitted area  $> 2\%$  of total active flank area; in the case of surface hardened gears, the pitted area  $> 0.5\%$  of total active flank area, or  $> 4\%$  of one particular tooth flank area. The  $\sigma_{Hlim}$  values are to correspond to a failure probability of 1% or less.

The endurance limit mainly depends on:

- (1) Material composition, cleanliness and defects;
- (2) Mechanical properties;
- (3) Residual stresses;
- (4) Hardening process, depth of hardened zone, hardness gradient;
- (5) Material structure (forged, rolled bar, cast).

Endurance limit for contact stress  $\sigma_{Hlim}$  is as given in **Table 6.3-1**. However, for materials having enough data showing their higher endurance limit, values larger than those given in the table may be allowed by the Society in consideration of factors (1) through (5) mentioned above.

(-3 to -5 are omitted)

#### 6 Roughness Factor, $Z_R$

The roughness factor  $Z_R$  accounts for the influence of surface roughness on surface endurance. The value for  $Z_R$  is to be calculated as follows:

$$Z_R = \left( \frac{3}{R_{Z10}} \right)^{C_{ZR}}$$

$$R_{Z10} = R_z \sqrt[3]{\frac{10}{\rho_{red}}}$$

$$R_Z = \frac{R_{Z1} + R_{Z2}}{2}$$

where

$R_{z1}, R_{z2}$  : Respective mean peak to valley roughness for pinions and wheels.

$\rho_{red}$  : Relative radius of curvature. The value for  $\rho_{red}$  is to be calculated by following formula:

$$\rho_{red} = \frac{\rho_1 \cdot \rho_2}{\rho_1 + \rho_2}$$

$$\rho_{1.2} = 0.5 \cdot d_{b1.2} \cdot \tan \alpha_{tw} \quad (\text{In cases where internal gears } d_b \text{ are negative})$$

In cases where the roughness stated is ~~an~~ an arithmetic mean roughness, i.e.  $R_a$  value, the conversion  $R_Z = 6R_a$  can be applied.

$$C_{ZR} = 0.32 - 0.0002\sigma_{Hlim} \quad (\text{In cases where } 850 \text{ N/mm}^2 \leq \sigma_{Hlim} \leq 1200 \text{ N/mm}^2)$$

$$= 0.15 \quad (\text{In cases where } \sigma_{Hlim} < 850 \text{ N/mm}^2)$$

$$= 0.08 \text{ (In cases where } \sigma_{Hlim} > 1200 \text{ N/mm}^2\text{)}$$

### 7 Hardness Ratio Factor, $Z_W$

The hardness ratio factor  $Z_W$  accounts for the increase in surface durability of soft steel gears meshing with significantly harder gears with smooth surfaces in the following cases:  $Z_W$  is to be applied to soft gears only. This factor mainly depends on:

- ~~(1) Hardness of soft gears;~~
- ~~(2) Alloying elements of soft gears;~~
- ~~(3) Tooth flank roughness of the harder gears. The hardness ratio factor  $Z_W$  is to be calculated as follows:~~

$$\begin{aligned} Z_W &= 1.2 \frac{HB - 130}{1700} \quad (130 \leq HB \leq 470) \\ &= 1.2 \quad (HB < 130) \\ &= 1.0 \quad (HB > 470) \end{aligned}$$

#### (1) Surface-hardened pinion with through-hardened wheel

$$\begin{aligned} Z_W &= 1.2 \cdot \left( \frac{3}{R_{zH}} \right)^{0.15} \quad (HB < 130) \\ &= \left( 1.2 - \frac{HB - 130}{1700} \right) \cdot \left( \frac{3}{R_{zH}} \right)^{0.15} \quad (130 \leq HB \leq 470) \\ &= \left( \frac{3}{R_{zH}} \right)^{0.15} \quad (HB > 470) \end{aligned}$$

where

$HB$  : Brinell hardness of the tooth flanks of the softer material gear of the pair

$R_{zH}$  : equivalent roughness ( $\mu\text{m}$ )

$$R_{zH} = \frac{R_{z1} \cdot (10 / \rho_{red})^{0.33} \cdot (R_{z1} / R_{z2})^{0.66}}{(v \cdot v_{40} / 1500)^{0.33}}$$

#### (2) Through-hardened pinion and wheel

When the pinion is substantially harder than the wheel, the work hardening effect increases the load capacity of the wheel flanks.  $Z_W$  applies to the wheel only, not to the pinion.

$$\begin{aligned} Z_W &= 1 \quad (HB_1 / HB_2 < 1.2) \\ &= 1 + \left( 0.00898 \frac{HB_1}{HB_2} - 0.00829 \right) \cdot (u - 1) \quad (1.2 \leq HB_1 / HB_2 \leq 1.7) \\ &= 1 + 0.00698 \cdot (u - 1) \quad (HB_1 / HB_2 > 1.7) \end{aligned}$$

$HB_{1,2}$  : Brinell hardness of the pinion and the wheel respectively.

If gear ratio  $u > 20$  then the value  $u = 20$  is to be used. In any case, if calculated  $Z_W < 1$  then the value  $Z_W = 1$  is to be used.

#### (3) In cases other than (1) and (2) above;

$$Z_W = 1$$

(-8 and -9 are omitted)

## 1.7 Bending Strength

Paragraph 1.7.1 has been amended as follows.

### 1.7.1 Equation

The tooth root bending stress  $\sigma_F$  and the permissible tooth root bending stress  $\sigma_{FP}$  are to be calculated separately for the pinion and the wheel. The criterion for tooth root bending strength, as given by the following equation, is that the tooth root bending stress in the tooth root fillet  $\sigma_F$  is to be equal to or less than the permissible tooth root bending stress  $\sigma_{FP}$ .

$$\sigma_F = \frac{F_t Y_F Y_S Y_\beta K_A K_V K_{F\alpha} K_{F\beta}}{b m_n} \leq \sigma_{FP}$$

$$\sigma_F = \frac{F_t}{b m_n} Y_F Y_S Y_\beta Y_{DT} K_A K_V K_{F\alpha} K_{F\beta} \leq \sigma_{FP}$$

However, the following definitions and equations apply only to those gears having a rim thickness greater than  $3.5 m_n$ . The results of calculations using the following method are acceptable for normal pressure angles up to  $25^\circ$  and reference helix angles up to  $30^\circ$ . In the case of larger pressure angles and larger helix angles, the method of calculation is to be given by the Society on a case by case basis.

### 1.7.2 Tooth Root Bending Stress for Pinion and Wheel

Sub-paragraph -1 has been amended as follows.

#### 1 Tooth Form Factor, $Y_F$

The tooth form factor  $Y_F$  accounts for the influence on nominal bending stress of the tooth form with load applied at the outer point of single pair tooth contact.  $Y_F$  is to be determined separately for the pinion and the wheel. In the case of helical gears, the form factors for gearing are to be determined in normal sections (i.e. for virtual spur gears with virtual numbers of teeth  $Z_n$ ). The value for  $Y_F$  is to be calculated as follows:

$$Y_F = \frac{6 \frac{h}{m_n} \cos \alpha_{Fen}}{\left( \frac{S_{Fn}}{m_n} \right)^2 \cos \alpha_n}$$

$S_{Fn}$ ,  $h_F$  and  $\alpha_{Fen}$  are to be calculated as follows:

$$S_{Fn} = m_n z_n \sin \left( \frac{\pi}{3} - \theta \right) + \sqrt{3} m_n \left( \frac{G}{\cos \theta} - \frac{\rho_{fp}}{m_n} \right)$$

$$G = \frac{\rho_{fp}}{m_n} - \frac{h_{fp}}{m_n} + x$$

$$\theta = \frac{2G}{z_n} \tan \theta - \frac{2}{z_n} \left( \frac{\pi}{2} - \frac{E}{m_n} \right) + \frac{\pi}{3}$$

$$E = \frac{\pi}{4} m_n - h_{fp} \tan \alpha_n + \frac{S_{Pr}}{\cos \alpha_n} - (1 - \sin \alpha_n) \frac{\rho_{fp}}{\cos \alpha_n}$$

$S_{pr}$  is illustrated in **Fig. 7.2-1**. However, in cases where racks are without undercuts, the value of  $S_{pr}$  is to be taken as zero.

$$h_F = \frac{m_n}{2} \left[ \left( \cos \gamma_e - \sin \gamma_e \tan \alpha_{Fen} \right) \frac{d_{en}}{m_n} - z_n \cos \left( \frac{\pi}{3} - \theta \right) - \frac{G}{\cos \theta} + \frac{\rho_{fp}}{m_n} \right]$$

$$\alpha_{Fen} = \alpha_{en} - \gamma_e$$

$$\gamma_e = \frac{0.5\pi + 2x \tan \alpha_n}{z_n} + \text{inv} \alpha_n - \text{inv} \alpha_{en}$$

$$\alpha_{en} = \arccos \left( \frac{d_{bn}}{d_{en}} \right)$$

$$d_{en} = 2 \frac{z}{|z|} \left\{ \left[ \sqrt{\left( \frac{d_{an}}{2} \right)^2 - \left( \frac{d_{bn}}{2} \right)^2} - \frac{\pi d \cos \beta \cos \alpha_n}{|z|} (\varepsilon_{an} - 1) \right]^2 + \left( \frac{d_{bn}}{2} \right)^2 \right\}^{\frac{1}{2}}$$

$$\varepsilon_{an} = \frac{\varepsilon_\alpha}{\cos^2 \beta_b}$$

$$\beta_b = \arccos \sqrt{1 - \sin^2 \beta \cos^2 \alpha_n}$$

$$d_{bn} = d_n \cos \alpha_n$$

$$d_n = m_n z_n$$

$$d_{an} = d_n + d_a - d$$

In the case of internal gears, the following coefficients used for determining the form factor are to be calculated as follows:

$$S_{Fn2} = \frac{m_n}{2} \left[ \frac{\pi}{4} + \frac{h_{fp2} - \rho_{fp2}}{m_n} \tan \alpha_n + \frac{\rho_{fp2} - S_{pr}}{m_n \cos \alpha_n} - \frac{\sqrt{3} \rho_{fp2}}{2 m_n} \right]$$

$$S_{Fn2} = m_n z_n \sin \left( \frac{\pi}{6} - \theta \right) + m_n \left( \frac{G}{\cos \theta} - \frac{\rho_{fp}}{m_n} \right)$$

$$h_{Fn2} = \frac{d_{en2} - d_{fn2}}{2} m_n \tan \alpha_n \left[ \frac{\pi}{4} + \left( \frac{h_{fp2}}{m_n} - \frac{d_{en2} - d_{fn2}}{2 m_n} \right) \tan \alpha_n \right] + \frac{\rho_{fp2}}{2}$$

$$h_{Fn2} = \frac{m_n}{2} \left[ \left( \cos \gamma_e - \sin \gamma_e \tan \alpha_{Fen} \right) \frac{d_{en}}{m_n} - z_n \cos \left( \frac{\pi}{6} - \theta \right) - \sqrt{3} \left( \frac{G}{\cos \theta} - \frac{\rho_{fp2}}{m_n} \right) \right]$$

$$d_{en2} = 2 \frac{z}{|z|} \left\{ \left[ \sqrt{\left(\frac{d_{an}}{2}\right)^2 - \left(\frac{d_{bn}}{2}\right)^2} - \frac{\pi d_2 \cos \beta \cos \alpha_n}{|z|} (\varepsilon_{cn} - 1) \right]^2 + \left(\frac{d_{bn2}}{2}\right)^2 \right\}^{\frac{1}{2}}$$

$$\frac{h_{JP2}}{2} = \frac{d_{n2} - d_{fn2}}{2}$$

Sub-paragraphs -4 and -5 have been added as follows.

#### 4 Rim thickness factor, $Y_B$

The rim thickness factor,  $Y_B$ , is a simplified factor used to de-rate thin rimmed gears. For critically loaded applications, this method should be replaced by a more comprehensive analysis. Factor  $Y_B$  is to be determined as follows:

(1) For external gears:

$$Y_B = 1.6 \cdot \ln \left( 2.242 \frac{h}{s_R} \right) \quad (0.5 < s_R / h < 1.2)$$

$$\underline{= 1} \quad (s_R / h \geq 1.2)$$

$s_R$  : rim thickness of external gears (mm)

$h$  : tooth height (mm)

The case  $s_R / h \leq 0.5$  is to be avoided.

(2) For internal gears:

$$Y_B = 1.15 \cdot \ln \left( 8.324 \frac{m_n}{s_R} \right) \quad (1.75 < s_R / m_n < 3.5)$$

$$\underline{= 1} \quad (s_R / m_n \geq 3.5)$$

$s_R$  : rim thickness of internal gears (mm)

The case  $s_R / m_n \leq 1.75$  is to be avoided.

#### 5 Deep tooth factor, $Y_{DT}$

The deep tooth factor,  $Y_{DT}$ , adjusts the tooth root stress to take into account high precision gears and contact ratios within the range of virtual contact ratio  $2.05 \leq \varepsilon_{cn} \leq 2.5$ .

$$\varepsilon_{cn} = \frac{\varepsilon_\alpha}{\cos^2 \beta_b}$$

Factor  $Y_{DT}$  is to be determined as follows:

$$Y_{DT} = 0.7 \quad (\text{ISO accuracy grade} \leq 4 \text{ and } \varepsilon_{cn} > 2.5)$$

$$Y_{DT} = 2.366 - 0.666 \cdot \varepsilon_{cn} \quad (\text{ISO accuracy grade} \leq 4 \text{ and } 2.05 < \varepsilon_{cn} \leq 2.5)$$

$$Y_{DT} = 1.0 \quad (\text{In all other cases})$$

### 1.7.3 Permissible Tooth Root Bending Stress, $\sigma_{FP}$

Sub-paragraph -5 has been amended as follows.

#### 5 Relative Notch Sensitivity Factor, $Y_{\delta reIT}$

The relative notch sensitivity factor  $Y_{\delta reIT}$  indicates the extent of the influence of concentrated stress on fatigue endurance limits. This factor mainly depends on materials and relative stress gradients. This factor is to be calculated as follows:

$$Y_{\delta reIT} = \frac{1 + 0.45\sqrt{\rho'(1 + 2q_s)}}{1 + 1.1\sqrt{\rho'}} \quad (\text{In all other cases})$$

$$Y_{\delta reIT} = \frac{1 + \sqrt{0.2\rho'(1 + 2q_s)}}{1 + \sqrt{1.2\rho'}}$$

$q_s$  : notch parameter

$\rho'$  : slip-layer thickness (mm)

However, the values to be used for  $\rho'$  are those given in **Table 7.3-2**.

Table 7.3-2 Values of  $\rho'$  (mm)

Materials	$\rho'$
Nitriding steels, surface or through hardened	0.1005
Steels having yield strength about 300 N/mm <sup>2</sup>	0.0833
Steels having yield strength about 400 N/mm <sup>2</sup>	0.0445
Through hardened steels having yield strength about 500 N/mm <sup>2</sup>	0.0281
Through hardened steels having yield strength 600 N/mm <sup>2</sup>	0.0194
Through hardened steels having $\sigma_{0.2}$ about 800 N/mm <sup>2</sup>	0.0064
Through hardened steels having $\sigma_{0.2}$ about 1000 N/mm <sup>2</sup>	0.0014
Surface hardening steels, surface hardened	0.0030

#### 6 Relative Surface Factor, $Y_{RreIT}$

The relative surface factor  $Y_{RreIT}$  takes into account the influence of surface conditions in tooth root fillets on root strength and mainly depends on peak to valley surface roughness. The value for  $Y_{RreIT}$  is to be determined as shown in **Table 7.3-3**.

Table 7.3-3 has been amended as follows.

Table 7.3-3 Values of Relative Surface Factor,  $Y_{RelT}$

Materials	$Y_{RelT}$
Case hardened steels, Through hardened steels ( $\sigma_B \geq 800 \text{ N/mm}^2$ )	1.120 (for $R_z < 1$ ) <del>1.675-0.53</del> $1.674-0.529 (R_z + 1)^{0.1}$ (for $1 \leq R_z \leq 40$ )
Normalized steels ( $\sigma_B < 800 \text{ N/mm}^2$ )	1.070 (for $R_z < 1$ ) <del>5.3-4.2</del> $5.306-4.203 (R_z + 1)^{0.01}$ (for $1 \leq R_z \leq 40$ )
Nitriding steels	1.025 (for $R_z < 1$ ) <del>4.3-3.26</del> $4.299-3.259 (R_z + 1)^{0.0058}$ (for $1 \leq R_z \leq 40$ )

Notes

- 1:  $R_z$  mean peak to valley roughness of tooth root fillets ( $\mu m$ ).
- 2: This method is only valid when scratches or similar defects deeper than  $2 R_z$  do not exist.
- 3: If the roughness stated is ~~a~~ an arithmetic mean roughness, i.e.  $R_a$  value, the approximation  $R_z = 6 R_a$  may be applied.

#### EFFECTIVE DATE AND APPLICATION (Amendment 3-2)

1. The effective date of the amendments is 1 January 2015.
2. Notwithstanding the amendments to the Guidance, the current requirements apply to all gears previously approved by the Society prior to the effective date for which no failure has occurred, and no changes related to strength, such as the scantlings of the gear meshes, materials, etc. have been made.